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Original scientific paper

Evaluation of remotely sensed precipitation product in a hydrological model of the Bednja watershed

In this paper, a statistical and spatial analysis of precipitation for the period 2000-2018 for the Bednja basin was performed, were the measured data from meteorological and/or rainfall stations of Croatian Meteorological and Hydrological Service (DHMZ) were compared with the data in form of remotely sensed precipitation product - CHIRPS (Climate Hazards Group InfraRed Precipitation with Station). The results of the analysis in the form of the annual sum, monthly distribution within the year and the spatial distribution and input data ratio over the basin show a good correlation between the measured and remotely sensed precipitation. In order to further evaluate the quality of the remotely sensed product, a SWAT hydrological runoff model was created.

Key words:

hydrological model, remote sensing, SWAT, CHIRPS, spatial precipitation analysis

Izvorni znanstveni rad

Karlo Leskovar, Petar Mrakužić, Hrvoje Meaški

Evaluacija daljinski opaženog produkta oborina u hidrološkom modelu sliva Bednje

U radu je provedena statistička i prostorna analiza oborina za period 2000. - 2018. godine na slivu rijeke Bednje, u svrhu čega su uspoređeni podaci s meteoroloških/kišomjernih postaja DHMZ-a s podacima u obliku daljinski opažanog oborinskog produkta - CHIRPS (Climate Hazards Group InfraRed Precipitation with Station). Rezultati analize u obliku hoda godišnjih visina oborina, mjesečnog hoda unutar godine i prostornog rasporeda te omjera ulaznih podataka iznad sliva pokazuju dobru korelaciju mjerene te daljinski opažene oborine. Kako bi se dodatno ocijenila kvaliteta daljinski opaženog produkta, izrađen je SWAT hidrološki model otjecanja.

Ključne riječi:

hidrološki model, daljinska opažanja, SWAT, CHIRPS, prostorna analiza oborina

Wissenschaftlicher Originalbeitrag

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Bewertung des entfernt beobachteten Niederschlagsprodukts im hydrologischen Modell des Einzugsgebiets des Flusses Bednja

In der Arbeit wurde eine statistische und räumliche Analyse des Niederschlags für den Zeitraum von 2000 bis 2018 im Einzugsgebiet des Flusses Bednja durchgeführt. Zu diesem Zweck wurden die Daten von Wetter- / Regenwassermessstationen des DHMZ (Staatliches Hydrometeorologisches Institut) mit Daten in Form eines fernbeobachteten Niederschlagsprodukts – CHIRPS (Climate Hazards InfraRed Precipitation with Station) verglichen. Die Ergebnisse der Analyse in Form des Verlaufs der jährlichen Niederschlagshöhen, des monatlichen Verlaufs innerhalb des Jahres und der räumlichen Verteilung sowie des Verhältnisses der eingehenden Daten oberhalb des Einzugsgebiets zeigen eine gute Korrelation zwischen dem gemessenen und dem entfernt beobachteten Niederschlag. Um die Qualität des entfernt beobachteten Produkts weiter zu bewerten, wurde ein hydrologisches SWAT-Abflussmodell entwickelt.

Schlüsselwörter:

hydrologisches Modell, Fernbeobachtung, SWAT, CHIRPS, räumliche Niederschlagsanalyse

1. Introduction

In recent times, we have increasingly been faced with extreme weather conditions, which may result in sharp rise in river water levels. Some of the recent events relating to Croatia, characterized by high water levels, are those experienced from May/June 2010 on the Danube, in November 2012 on the Drava and Mura, and in May 2014 on the Sava River. The theme of this paper is the Bednja River basin, which has already been the subject of research with the aim of making flood hazard maps, due to the presence of numerous local communities along its watercourse [1].

However, in this paper, the water wave volume was crucial for the conducted research, as an alternative approach in hydrological modelling due to the characteristics of smaller catchments, where water waves are often caused by precipitation over the entire catchment area [2, 3]. Furthermore, due to negligible runoff coefficient variations, resulting in a constant ratio of effective to total precipitation [4], the water wave could in this case be a good indicator when comparing the precipitation over the basin. Several parameters are important for the formation of water waves, the most notable being: high-intensity precipitation, inflow water wave, spatial distribution of rain over the catchment area, type of land cover and soil type within the basin, relief, etc. The water wave is defined by several key characteristics: peak flow, water wave duration, water wave rise and fall time, and/or water wave volume [5, 6]. In the analysis of precipitation over the basin or the development of hydrological models, the existence of a

sufficient number of measuring points is very important, but their distribution within the basin is also highly significant [7]. However, the number of measuring stations is often insufficient in rural and hilly areas - partly due to sparse population density, and partly due to inaccessible terrain - which is a serious challenge for accurate hydrological modelling.

As the Bednja River basin is not affected by the lack of measuring stations, it is quite suitable for assessing the possibility of applying the remotely sensed precipitation product (CHIRPS -Climate Hazards Group InfraRed Precipitation with Station) [8] in hydrological modelling using the SWAT (Soil and Water Assessment Tool) hydrological model [9]. The SWAT hydrological model has been widely applied for the purposes of hydrological modelling of basins [9–11], for measuring the impact of climate change on basins [12], and also for comparing different precipitation input data [13, 14]. The aim of this paper is to compare precipitation traditionally measured at weather (rainfall) stations of DHMZ with the remotely sensed precipitation product - CHIRPS in the form of statistical analysis, time course, intra-year distribution and spatial distribution above the Bednja basin. The application of the SWAT hydrological model has not been widely investigated in Croatia, i.e. only one paper [15] deals with the SWAT model implementation in Croatia, while the application of remotely observed precipitation products in hydrological modelling is completely unexplored in Croatia. Therefore, the possibility of applying the SWAT hydrological model with the measured and remotely sensed precipitation input data was tested as part of this research on the example of the Bednja River basin.



Figure 1. Geographical position of the Bednja River basin

2. Data and methods

2.1 Hydrogeological characteristics

The investigated area is situated in north-west of Croatia and includes the Bednja River basin (Figure 1), which is a part of the Drava river basin. In a broader context it is a part of the Danube basin. The main course of the Bednja River is about 103 km long [16]. The Bednja River runs in the west-east direction throughout its course, except for a very small deviation near Novi Marof where it first runs southward and then turns toward the north.

Regarding the hydrogeological features, three basic parts of the basin can be distinguished [17, 18]. The first part is the area of the underlying mountains (Ivanščica, Kalničko gorje and Ravna gora) which is built of carbonate rocks - mostly dolomite of secondary porosity dating back to the Mesozoic Era. The thickness of the carbonate aquifer is estimated at several hundred meters [17], and the permeability of these rocks is estimated at 3 to 25 % [19]. Other hydrogeological parameters have not so far been sufficiently studied, but it is known that folds and faults give basic structural features to this part of the catchment area. The second part is the area composed of sedimentary complexes of the Tertiary Period, which are the result of leaching and erosion of older rocks. These sediments are associated with hilly hills and smaller stream valleys on the slopes of the underlying mountains.

The third part is the area composed of the Quaternary age deposits in the lowland area along the Bednja River. Today, this area is a fundamental feature of the Bednja River because gravel, sand and clays of Holocene age are deposited in the valley of the river and its tributaries, and they represent a significant alluvium of Varaždin County. This alluvium is primarily formed by geological weathering of older rocks of Mesozoic and Tertiary age and through accumulation of this material in river valleys. The base is dominated by gravel and sand, and the granules are predominantly made of guartz; there are also traces of eruptive rocks and fragments of limestone and dolomite [20]. From the hydrogeological aspect, alluvial sediments of the Bednja River form aquifers of intergranular porosity, of small thickness, and of laterally and vertically heterogeneous composition. Since fine-grained particles dominate, the permeability of these deposits is low, and groundwater recharging occurs primarily by infiltration of precipitation and seepage from watercourses [21].

The general flow of groundwater within the Bednja River basin follows the direction of the Bednja River flow and the groundwater flow is on a regional scale controlled by recent structural features, i.e., by faults and geological structures [22].

2.2. Hydrological characteristics

The Bednja River basin is defined by a topographic catchment. The catchment area of 596 km² and the mean river basin width of about 5.8 km were defined in previous investigations [17]. The catchment area is dominantly elongated and spreads from Trakošćan in the west to Ludbreg in the east. It is a predominantly lowland area bordered on the west by Maceljsko gorje mountains, on the south by Ivanščica mountain and Kalničko gorje mountains, and on the north by smaller hills that represent a water divide towards the Plitvice watercourse. To the east is the confluence with the Drava River.

The very beginning of the Bednja River course is not precisely defined because there are various literary references - a stream that emerges at Brezova gora, a source in Ravna gora near the municipality of Bednjica, a source in Kamena gorica, an outflow of water from Lake Trakošćan. The confluence of the Bednja and the Drava River is located near the settlement of Mali Bukovec. In its longitudinal profile, the Bednja River is predominantly a lowland river with a very small longitudinal slope. However, the associated basin is almost exclusively hilly [16]. Along the course of the Bednja, one can distinguish the upper course (to the mouth of the Željeznica), the middle course (to the mouth of the Velinečki creek), and the lower course to the mouth of the Drava River. The upper course is fan-shaped, which together with the existing rainfall intensity results in a large and rapid concentration of inflow that regularly forms flood waves [1]. In the entire upper and middle course, the Bednja riverbed is formed of clay material with added mixtures of sand and mud. The material of the riverbed is highly susceptible to erosion, and so the faster flow was solved by widening the profile, as well as by cutting meanders. In its lower course the Bednja runs through a distinctly flat area, mostly composed of arable land and meadows. Erosion processes are present throughout the basin.

There are five active hydrological stations in the Bednja River basin (Table 1): Lepoglava, Željeznica, Ključ, Tuhovec, and Ludbreg. The Lepoglava hydrological station started operating in 1986, and a limnigraph (water level recorder) was installed in 2005. The Željeznica hydrological station started operating in 1958, a limnigraph was installed in 1960, and a remote water level alarm was added in 2006. The Ključ hydrological station started operating in 1986, and an electronic limnigraph has been in operation since 2002. The Tuhovec hydrological station started operating in 1957, was abandoned in 1975, its operation

Table 1. Basic statistical indicators of dail	runoff at the Bednia River hydrold	gical stations (2000 2018.)
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Indicators Water stations	Data points	Mean	St. deviation	Min.	25 %	50 %	75 %	Max.
Lepoglava	6940	1.21	2.70	0.03	0.24	0.50	1.07	44.7
Željeznica	6940	3.30	6.38	0.21	0.80	1.44	2.91	123.0
Ključ	6435	4.91	8.86	0.33	1.33	2.21	4.20	90.2
Tuhovec	6549	5.08	9.19	0.55	1.51	2.31	4.35	103.0
Ludbreg	6940	6.10	10.09	0.43	1.90	2.95	5.68	116.0

resumed in 1979, and an electronic limnigraph was installed in 2003. The Ludbreg water meter station started operating in 1938, and a remote water level alarm was added in 2006.

According to hydrological research conducted so far [1], the Bednja is a very torrential watercourse, and the flow directly depends on the volume of precipitation, but also on the melting of snow in the area around the source of the Bednja. The highest runoff occurs in spring (March and April) when the snow melts and spring storms are at their strongest [23]. Storm showers (usually occurring in August and September) are also common, causing sudden extreme increase in flow, as well as prolonged and heavy rains in September and October. By analysing the flow at hydrological stations along the Bednja River in the 2000 - 2018 period (Table 1), the lowest flow (0.032 m³/s) was measured on 8 August 2000 at the upstream-most station in Lepoglava, while the highest flow rate (123 m³/s) was measured on 20 September 2017 at the Željeznica station. Interestingly, on the same day, 76.1 m³/s was registered at the Ludbreg station, and 85.4 m³/s in the following day, which is probably the result of the riverbed overtopping upstream of the Ludbreg station. The highest flow rate at the Ludbreg station, amounting to 116 m³/s, was measured on 14 September 2014. The conducted analysis reveals that the number of extreme events in autumn has been increasing in recent years, which partly shows a somewhat greater impact of rain, and somewhat lower impact of snow on the runoff of the Bednja River.

2.3. Weather data and characteristics

Weather data for the period from 2000 to 2018 were obtained by the Croatian Meteorological and Hydrological Service [24] (hereinafter DHMZ). In the area of the Bednja basin itself, there are three climatological (Bednja, Novi Marof and Ludbreg) and three precipitation gauge stations (Klenovnik, Varaždinske Toplice and Kalnički Ljubelj). In the immediate vicinity of the basin there are seven more precipitation gauge stations (Križovljan, Donji Macelj, Kalnik, Gornja Rijeka, Šemovec, Rasinja and Legrad) and the main weather station in Varaždin [24] (Figure 1). The data from all fourteen stations were used in the statistical and spatial analysis of precipitation so as to enable determination of average values.

According to data from the Ludbreg weather station, the climate in the wider Ludbreg area is moderately warm-rainy, featuring warm summers with the temperature in the warmest month not exceeding 22 ° C and the temperatures in the coldest month ranging between -3 ° C and 18 ° C. There are no dry periods. Precipitation varies from year to year, for example in 2012 it was 716.9 mm, in 2013 1196.8 mm, and in 2014 1376.4 mm. 55 - 60 % of the total precipitation is registered in the warm part of the year (April - September), and 40 - 45 % in the cold part of the year (October - March). Snow cover can be expected on 45 to 50 days during the winter, and a minimum 1 cm of snow cover can be expected during ten or more days. The winds of the southern and southwestern and northern and northeaster quadrants are dominant in the area. Spring is the windiest, while low-frequency winds occur during the summer.

CHIRPS [8] data can be downloaded in several different raster formats (.tiff, .netcdf, .bil and .png), In this study, we used the global coverage data in a daily step of spatial resolution 0.05 ° in .netcdf format. Nineteen files were downloaded since .netcdf data are multilayer rasters, where each layer represents one measurement (in this case one day a year) (2000–2018).

	Data points	Mean	St. devijacija	Min	25 %	50 %	75 %	Max.
Bednja	4628	2.88	7.51	0	0	0	1.1	80.0
Ludbreg	6940	2.45	6.51	0	0	0	1.1	83.6
Novi Marof	6850	2.36	6.12	0	0	0	1.0	68.1
Varaždin	6940	2.32	6.29	0	0	0	0.9	95.5
Donji Macelj	6940	2.82	7.46	0	0	0	1.0	90.2
Gornja Rijeka	6940	2.54	6.79	0	0	0	1.2	85.8
Kalnički Ljubelj	6940	2.79	7.34	0	0	0	1.0	89.3
Kalnik	6940	2.67	7.05	0	0	0	1.2	79.3
Klenovnik	6573	2.74	6.90	0	0	0	1.2	94.7
Križovljan	6928	2.57	6.62	0	0	0	1.0	99.2
Legrad	6940	2.08	5.54	0	0	0	0.8	64.6
Rasinja	6940	2.25	6.07	0	0	0	0.9	98.2
Šemovec	6911	2.28	6.22	0	0	0	0.9	92.3
Varaždinske Toplice	6940	2.57	6.95	0	0	0	1.0	88.8
METEO_AVG	6940	2.51	6.06	0	0	0.01	1.5	80.8
CHIRPS_AVG	6940	2.47	6.43	0	0	0	1.4	98.4

Table 2. Basic statistical indicators of measured (DHMZ) and remotely sensed (CHIRPS) daily precipitation (2000. - 2018.)

Table 3. Input data required by SWA	T hydrological model
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Input data	Source	Spatial resolution
Digital elevation model (DEM)	Copernicus - EU DEM v 1.1. https://land.copernicus.eu/imagery-in-situ/eu-dem/eu-dem-v1.1	25 m x 25 m
Soil type	EEA - European Soil Data Centre (ESDAC) [27]. https://esdac.jrc.ec.europa.eu/	1 km x 1 km
Land cover and Land Use data	European Environment Agency. Corine Land Cover (CLC) 2012 ver. 2020. https://land.copernicus.eu/pan-european/corine-land-cover/clc-2012	100 m x 100 m
Precipitation	Observed – DHMZ, 2020, 1 main, 3 climatological, 10 precipitation stations Daljinsko opažanje - Climate Hazards Group InfraRed Precipitation with Station [28]. <u>ftp://ftp.chg.ucsb.edu/pub/org/chg/products/CHIRPS-2.0</u>	- /- 0.05° x 0.05°
Climatological data – temperature, relative humidity, wind speed	Observed – DHMZ, 2020, 1 main, 3 climatological stations	- /
Climatological data – solar radiation	Remotely sensed - National Centers for Environmental Prediction (NCEP) [29] - solar radiation. <u>https://globalweather.tamu.edu/#pubs</u>	0.5° x 0.5°

2.4. SWAT model and input data

SWAT (Soil & Water Assessment Tool) [9, 25] is a physics-based hydrological model developed for the purpose of evaluating changes in hydrological processes, river erosion and water quality in large basins [10, 26]. Model simulation is possible in annual, monthly, daily and hourly time steps. Structurally, the model divides the basin into sub-basins and further into hydrological units - HRU (Hydrologic Response Units), which are characterized by unique properties related to land use and cover (Land Use / Land Cover), soil type (Soil), and topographic characteristics - Slope. The hydrological cycle within each HRU is determined by water balance (Eq. 1), which is controlled by weather parameters, precipitation, maximum and minimum daily air temperature, relative humidity, wind speed, and solar radiation.

$$SW_{t} = SW + \sum_{t=1}^{t} (R_{i} - Q_{i} - ET_{i} - P_{i} - QR_{i})$$
(1)

where:

 SW_t - the volume of water in the unit volume of soil at time t_i

- *SW* the volume of water in soil at time *t*-1
- t time
- R -the precipitation
- Q the runoff
- ET the evapotranspiration
- P the percolation into deep aquifer,
- QR the seepage from shallow aquifer to the watercourse. All parameters are in mm [9].

While creating the model, the SWAT2012 version was used together with the ArcSWAT 2012.10.23 plugin for ArcMap, which enabled creation of a SWAT model of the basin in a graphical interface. The list of input data and sources is given in Table 3.

A digital elevation model with a spatial resolution of 25 x 25 m was used as an input parameter for determining the direction of flow and division into sub-basins. Land cover / Land use data (Corine Land Cover) and the data on soil type according to FAO85 classification were used to determine the HRUs. In addition to the land cover and soil type data, SWAT uses a digital elevation model for the classification of terrain slope when dividing into HRUs. Given the predominantly lowland character of the basin and a moderate difference between the highest and lowest points in the basin (approx. 900 m), the slopes of the terrain were divided into three classes. Thus, the Bednja river basin was divided into 12 sub-basins and 148 HRUs.

2.5. Filling missing time-series data

Since SWAT simulations require continuous input of data, it was necessary to find a sufficiently long period without significant gaps in the input of data and, when necessary, to fill in the missing data, either by applying appropriate interpolation procedures or by selecting other available data.

An ideal time period, with minimal interruptions of measurements at individual stations, was determined by overlapping climatological data from all measuring stations within the basin. This period started on 1 January 2008 and ended on 31 December 2017. Additional analysis of data from measuring stations situated in the basin (Klenovnik, Bednja, Kalnički Ljubelj, Varaždinske Toplice, Ludbreg, and Novi Marof), showed that there are frequent data measurement interruptions at the climatological station Novi Marof, which may present difficulties in developing a hydrological model, and that some time series are missing at the Ludbreg station.

For the weather station Novi Marof, it was determined that the stations Varaždinske Toplice and Kalnički Ljubelj have complete observation data, and so these data were entered for the Novi Marof station in the model. In the case of the weather station Građevinar 4/2021



Figure 2. Correlation of weather stations Ludbreg and Varaždin in the period July-September 2017

Ludbreg, it was established that no other station can be used as its replacement. However, an additional analysis showed a very good correlation with the nearby weather station Varaždin (correlation coefficient 0.95) and so the data from that station were used to supplement and interpolate the data missing at the Ludbreg station (Figure 2).

Solar radiation data (W/m²) were not available (insolation data were obtained, which is not enough to produce a SWAT model), and so the option of simulating data according to the database was used. Namely, the entry of the required climate data into the SWAT model is possible as a direct time series or as a simulation. SWAT simulations of climate data are performed based on databases and, in this case, the Climate Forecast System Reanalysis [29] (hereinafter CFSR) database was used, as it had been successfully used in several studies [14, 30–32] as the only input parameter in the SWAT model.

2.6. SWAT-CUP calibration tool

The SWAT-CUP (SWAT - Calibration Uncertainty Programs) [33] is a program designed to calibrate and assess sensitivity parameters (Sensitivity Analysis) of the SWAT model. The SUFI-2 (Sequential Uncertainty Fitting 2) method was used in this paper. The SUFI-2 offers up to 10 different statistical indicators for the calibration of quality. in this paper, the coincidence of modelled and observed flows was used, and the coefficient of determination R² (Eq. 2) and coefficient NSE (Eq. 3) (Nash-Sutcliffe efficiency) were selected as the main indicators [34]. R² [35] significantly depends on peak flows, and so it was chosen as a significant indicator of the quality of torrent models such as that involving the Bednja.

$$R^{2} = \frac{\left[\sum_{i} \left(Q_{m,i} - \bar{Q}_{m}\right) \left(Q_{s,i} - \bar{Q}_{s}\right)\right]^{2}}{\sum_{i} \left(Q_{m,i} - \bar{Q}_{m}\right)^{2} \sum_{i} \left(Q_{s,i} - \bar{Q}_{s}\right)^{2}}$$
(2)

where:

 $\begin{array}{ll} Q_{m,i} & - \mbox{ the measured runoff over time } i \\ \overline{Q}_m & - \mbox{ the mean observed runoff } \\ Q_{s,i} & - \mbox{ the modelled runoff over time } i \\ \overline{Q}_s & - \mbox{ the mean modelled runoff.} \end{array}$

NSE (Eq. 3) determines the importance of residual variance between the modelled and observed runoff [34, 35].

$$NSE = 1 - \frac{\sum_{i} (Q_{m} - Q_{s})_{i}^{2}}{\sum_{i} (Q_{m,i} - \overline{Q}_{m})^{2}}$$
(3)

where:

 $\begin{array}{l} Q_{m,i} = Q_m \ - \ \text{the observed runoff over time } i \\ Q_{\underline{s}} & - \ \text{the modelled runoff over time } i \\ \overline{Q}_m & - \ \text{the mean observed runoff.} \end{array}$

All R² [35] and NSE [36] values above 0.5 are considered satisfactory, while NSE values between 0.75 point to an extremely reliable model [37]. The p-factor and the r-factor – parameters directly related to SWAT-CUP – were also evaluated. The P-factor is a measure of the amount of data within the 95PPU band (simulated flow values between 2.5 and 97.5 % confidence), while the r-factor indicates the width of the 95PPU band [10]. According to [10], p-factor values between 0.7 and 0.75 are considered adequate in runoff modelling [10] while, according to the same author [38, 39], r-factor values of around 1.5 are considered desirable.

Comparison of precipitation input parameters observed at DHMZ stations and remotely sensed CHIRPS product

3.1. Statistical precipitation analysis

Mean values of remotely observed precipitation for the Bednja basin were compared (arithmetic mean of 75 raster points within and along the basin) with the precipitation measured at GMP Varaždin, and at DHMZ climatological and precipitation gauge stations (arithmetic mean of 14 stations (Figure 1) for the period 2000 - 2018) in order to assess the possibility of applying the remotely sensed precipitation (CHIRPS product). Statistical daily precipitation values (Table 2), mean values of measured precipitation at the rain gauge stations (METEO_AVG), and mean values of CHIRPS remotely observed precipitation (CHIRPS_AVG) were also determined.



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Figure 4. Monthly precipitation values during the year observed at DHMZ stations, mean values of all observing stations (METEO_AVG) and mean values of remotely sense points (CHIRPS_AVG) – 2000 – 2018

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Table 4. Basic statistical indicators of mean observed precipitation values (DHMZ) and mean remotely sensed precipitation (CHIRPS) – 2000 – 2018 – monthly, yearly and monthly per season time step

	Data points	Mean	St. dev.	Min.	25 %	50 %	75 %	Max.
METEO_mj	228	76.37	45.80	0.42	45.94	70.19	102.11	257.93
CHIRPS_mj	228	75.12	37.78	6.69	51.67	70.41	92.94	214.31
METEO_DRY_mj	114	64.00	40.91	0.42	35.21	58.09	91.32	223.44
METEO_WET_mj	114	88.75	47.24	4.30	57.11	80.35	115.18	257.93
CHIRPS_DRY_mj	114	58.30	29.94	6.69	36.31	56.11	76.27	174.82
CHIRPS_WET_mj	114	91.94	37.41	23.68	64.56	85.88	110.99	214.31
METEO_god	19	916.50	192.22	548.26	840.94	934.07	965.11	1314.42
CHIRPS_god	19	901.48	133.36	589.87	844.21	913.82	963.96	1179.14



Figure 5. Spatial interpolation of mean daily precipitation [mm]; CHIRPS product (left) and measured precipitation (right); yearly (upper), dry season (middle); wet season (bottom)

The remotely observed product for the observed area slightly underestimates annual precipitation for the period 2000-2018, with a lower scatter of data (133.96 vs. 192.22) (Table 4). Furthermore, the measured precipitation has extremes (minimum and maximum values) that are more pronounced, while the guartiles are very similar for both modes of observation. Graphical representation of the total annual precipitation (Figure 3) additionally confirms the good match between the mean remotely observed precipitation (CHIRPS product) and the arithmetic mean of precipitation observed at weather stations and/or precipitation stations. It should be noted that there is a certain deviation of remotely sensed precipitation in rainier years (2010, 2013, 2014). The median amount of mean monthly precipitation at the measuring stations is almost identical to the median mean monthly precipitation of the remotely observed product (Figure 4), while the arithmetic mean is slightly lower for the remotely sensed precipitation compared to the observed precipitation.

The analysis of monthly precipitation values throughout the year (Figure 4) shows that the hydrological year in the observed basin is characterized by two periods, i.e. the wet period (May - October) and the dry period (November - April). The wet part of the year is characterized



Figure 6. Ratio of remotely sensed product (CHIRPS) to measured precipitation (DHMZ); yearly (top), dry season (middle), wet season (bottom)

by the months with total monthly precipitation in excess of 70 mm, locally reaching as many as 120 mm in September at some stations, while average monthly values during the dry part of the year range between 60-65 mm per month. The month with the highest precipitation is September (P_m _September = 113 mm), while the lowest values are recorded in January (P_m _January = 51 mm) and March (P_m _March = 58 mm).

3.2. Spatial precipitation analysis

A spatial analysis was conducted in order to show more clearly the variation of precipitation values over the basin. The spatial distribution analysis consists of the analysis of the mean daily precipitation in the observed period, the analysis of the mean daily precipitation during the dry season, and the analysis of the mean daily precipitation during the wet part of the year (Figure 5) for each of the observation/measurement methods, which makes up a total of six components. For this purpose, the average daily precipitation in the observed period was determined on an annual basis, during the dry part of the year, and during the wet part of the year. The results were calculated using the Python 3 script, while the visualization was conducted in ArcGIS using spatial interpolation and the kriging method [40].

Visual interpretation shows a similar spatial distribution of precipitation values above the basin, with a slightly larger range of minimum and maximum mean daily precipitation values for the remotely sensed product (1.74 mm - 3.48 mm) compared to climatological measurements (1.88 mm - 3.42 mm). Furthermore, the mean precipitation on an annual basis (Figure 5 - top) and during the dry part of the year (Figure 5 middle) generated with the remotely observed product resulted in a much more uniform spatial distribution of precipitation measured above the basin, which may be due to more points in the grid during interpolation. In meteorological measurements, spatial variations are somewhat more pronounced along the western hilly parts and along the eastern lowland part around Ludbreg. In the wet part of the year, the situation changes, i.e., the spatial distribution of the remotely sensed product is very similar to that of meteorological measurements - with relatively greater precipitation along the western hilly part of the basin, while downstream precipitation decreases linearly with both types of input data.

In the final step, the ratio of the remotely sensed product (CHIRPS) to precipitation measurements was analysed, so that the raster ratio of remotely sensed product CHIRPS and precipitation measured at DHMZ stations was calculated. The coincidence of the remotely sensed product with the measured precipitation is better when the ratio is closer to 1. A ratio greater than 1 points to the overestimation of the remotely sensed product in relation to weather measurements, while a ratio smaller than 1 indicates areas where the remotely observed product shows lower precipitation values compared to weather measurements.

With average daily precipitation at the annual level and when observing the dry period, a very good overlap can be observed in the central part of the basin, around the area of Novi Marof, while along the marginal parts, the remotely sensed product shows lower precipitation values. When observing the wet part of the year, the situation is reversed, and so in the central part the overestimation of (blue) remotely sensed product (CHIRPS) is visible, while in peripheral parts of the basin the ratio is around one, which indicates a very good overlap between remote observations and weather measurements. (Figure 6).

4. Hydrological runoff model results and discussion

The possibility of applying the remotely sensed precipitation (CHIRPS product) in the observation of the water wave volume was tested using the SWAT hydrological model. As very often the model does not give a satisfactory result in its initial form, it is important to calibrate the model [10, 41, 42], and the result is then validated on an independent time period that is not covered by previous calibration.

Before performing such calibration/validation, it is important to select appropriate time periods. Therefore, the hydrograph of the most downstream hydrological station in the hydrological model (Ludbreg) was analysed. For the high quality and reliability of the calibration/validation process, it is very important to select periods that contain a similar number of wet and dry years, i.e., they should be statistically as similar as possible [5, 20] (and personal communication with Dr. K. Abbaspour). Wet years are characterized by hydrographs with the pronounced peak flow and a pronounced duration (higher volume of the water wave), while dry years are characterized by hydrographs with a less pronounced peak flow and, in general, with a very low base flow [2]. The hydrograph of the Ludbreg station was analysed both visually and statistically. The period from 2008 to 2014 was selected as the calibration period ($Q_m = 6.76 \text{ m}^3/\text{s}$, $Q_stdev = 11.66 \text{ m}^3/\text{s}$) while the reliability of the model was assessed in the period from 2015 to 2017. (Q m = $6.62 \text{ m}^3/\text{s}$, Q stdev = $11.30 \text{ m}^3/\text{s}$). The calibration period is characterized by seven dynamic years, 2008 and 2010 representing years of moderate flows, 2012 a dry year, 2011 an extremely dry year, while 2009, 2013 and 2014 (Figure 7) represent years with very high flow values. In the validation period, 2015 represents an extremely wet year, 2016 a moderate year, and 2017 a dry year (Figure 7).

Table 5. Parameters and ranges used during calibration of the SWAT model [46]

Parameter	Parameter description	Calibration range
vALPHA_BF.gw	Baseflow alpha factor (1/days)	0.0 to 1.0
vCANMX.hru	Maximum canopy storage (mm H ₂ 0)	0 to 15
rCN2.mgt	Soil conservation services (SCS) runoff curve number	-0.15 to 0.15
vESCO.hru	Soil evaporation compensation coefficient	0 to 1
vGWQMN.gw	Threshold depth of water in shallow aquifer for return flow (mm)	0 to 1000
rSOL_K().sol	Saturated hydraulic conductivity (mm/hr)	-0.15 to 0.15
aREVAPMN.gw	Threshold depth of water in the shallow aquifer for "revap" or percolation to occur (mm $\rm H_20)$	-1000 to 1000
vGW_REVAP.gw	Groundwater "revap" coefficient	0.02 to 0.2
aGW_DELAY.gw	Delay time for aquifer recharge (days)	-150 to 250
vSMTMP.bsn	Snowmelt temperature (°C)	-5 to 5
vSFTMP.bsn	Snowfall temperature (°C)	-5 to 5

Measuring station	Calibration				Validation			
	p-factor	r-factor	R ²	NSE	p-factor	r-factor	R ²	NSE
Ludbreg_m	0.85	1.11	0.86	0.84	1.00	1.31	0.91	0.89
Željeznica_m	0.88	1.26	0.83	0.74	1.00	1.35	0.92	0.91
Lepoglava_m	0.85	1.11	0.77	0.74	0.97	1.22	0.91	0.90
Ludbreg_ch	0.81	1.00	0.89	0.85	0.81	1.10	0.80	0.73
Željeznica_ch	0.90	1.11	0.84	0.84	0.89	1.09	0.82	0.81
Lepoglava_ch	0.83	0.97	0.78	0.77	0.69	0.94	0.73	0.67

Table 6. Statistical indicators of the calibration and validation results; stations with suffix -m indicate the model with measured precipitation input data, while the stations with suffix -ch indicate the model wit remotely sensed CHIRPS data

To ensure optimum results, model calibration was performed at three points (measuring stations): Lepoglava, Željeznica, and Ludbreg. The reason for this is to consider the lower flows in the upstream part of the basin (Lepoglava station), the boundary between the upper and middle part of the river (Željeznica), and the last measuring station on the Bednja River (Ludbreg), which is also the outlet of the hydrological model.

The process of calibrating the model with SWAT-CUP begins with Sensitivity Analysis [44]. In this step, the model is simulated with several parameters that include the processes observed in the basin, considering the physical characteristics of the basin, and especially the ranges of selected parameters to find the most sensitive ones (Table 5). This information is then used to calibrate the model [10, 38, 44, 45].

Calibration of SUFI-2 parameters by

the SWAT-CUP software algorithm can be performed in one of three ways: relative change of r__, absolute change of a__, and replacement of parameters with a new value of v__ [33, 45]. Relative change (i.e., r__CN -0.2 - 0.2) means the relative change of the CN number of the SCS runoff curve within a single hydrological unit (HRU - Hydrologic Response Unit) within the range - / + 20 % and within the physically realistic limits of the CN curve number in general. An absolute change (i.e., a___ GW_DELAY in the range of -150 to +250) indicates a change in the time period of aquifer saturation ("filling") for a random value in the range of -150 to +250 days, i.e., the initial number of days (depending on the type of soil, vegetation cover, etc.) is increased (or decreased) by a random value from a selected range. Parameter replacement, v__ indicates a change of an existing parameter (i.e., v__GWQMN 0 - 1000), where the initial depth of water in a shallow aquifer (depending on soil type, vegetation cover, etc.) is replaced by a random value from a selected range. It should be noted that the number of values



Figure 7. Hydrograph of modelled runoff for the Ludbreg station; with measured precipitation input (upper), with CHIRPS remotely sensed precipitation input (bottom)

from the selected range depends on the number of selected model simulations, i.e., if the number of simulations is 1000, the range is divided into 1000 parts and the mean value of each part is taken with the random value of all other parameters in the simulation.

At the end, the statistical indicators of the simulation are calculated (Table 6) and the parameters of the simulation that gives the smallest statistical error are selected as the "best simulation" (red line - Figure 7), while the whole range of possible runoff values depends on the parameters shown by the area 95PPU (green - Figure 7.).

After analysis of statistical calibration and validation parameters presented in Table 6. and according to the proposed values of the coefficients R², NSE, p-factor and r-factor for SWAT hydrological model [10, 35–39], it can be concluded that the model provides a reliable result. This is supported by the fact that the NSE coefficient is greater than 0.5 [35]. The assumption is also that extending of the calibration period would average the results,

but this is beyond the scope of this paper. It is interesting to note that in the calibration process, the model with weatherly observed precipitation gives a slightly worse result, while during the validation period the situation is reversed.

Compared with similar studies in other areas [13], the obtained results show that the remotely sensed product CHIRPS could be a valid input to the SWAT hydrological model for small basins in Croatia, in the cases when a low density of precipitation gauging stations, or interruptions in time series, are present.

However, this approach to modelling has certain limitations, which are noticeable in the visual interpretation of the runoff hydrograph of the SWAT hydrological model, as shown in Figure 7. It can be seen that the meteorologically measured precipitation as an input parameter of the SWAT hydrological model better describes peak flows in wet years (i.e., 2013 or January 2015), where CHIRPS, due to an error in the observed precipitation volume (Figure 3.), does not achieve the actual peak flows recorded in that month. If we look at the years in which the CHIRPS product nicely overlaps with volumes of meteorologically measured precipitation, the error recorded in the model is also lower. The situation changes in dry years (periods), when the CHIRPS product, due to a larger number of observation points (raster), describes much better the minimum amounts of precipitation, which is reflected in a better representation of the base flow. This feature is also an advantage of remotely observed products in areas with extremely low density of weather stations. Due to that, they can give much more reliable results than the meteorologically measured precipitation, because they can transfer the spatial distribution of the precipitation over the basin in a more realistic manner.

The obtained data show that the CHIRPS product describes well the time of rising and falling of the water wave in both wet and dry

REFERENCES

- Paladin, M., Vidaković Šutić, R., Vrcelj, B., Ričković, V.: Izrada karata opasnosti i izračun šteta na slivu rijeke Bednje, (urednici: Biondić, D., Holjević, D., Vizner, M.), Hrvatske vode na investicijskom valu, Hrvatske vode: Opatija; 2015.
- Žugaj, R.: Hidrologija, Sveučilište u Zagrebu, Rudarsko-geološkonaftni fakultet: Zagreb; 2000.
- [3] Žugaj, R.: Velike vode malih slivova, Sveučilište u Zagrebu, Rudarsko-geološko-naftni fakultet: Zagreb; 2010.
- [4] Wanielista, MP., Kersten, R., Ealgin, R.: Hydrology : water quantity and quality control, 2nd ed. John Wiley & Sons: New York; (1997) pp. 567
- [5] Gilja, G., Ocvirk, E., Kuspilić, N.: Joint probability analysis of flood hazard at river confluences using bivariate copulas, GRADEVINAR, 70 (2018) 4, pp. 267-75, https://doi.org/10.14256/JCE.2173.2017
- [6] Ožanić, N., Karleuša, B., Orbanić, J., Žufić, E., Žic, E.: Hidrogrami velikih vodenih valova - primjer hidrološke obrade za akumulaciju Križ, In: Gereš D, urednik. 3 Hrvatska konferencija o vodama hrvatske vode u 21 stoljeću, Hrvatske vode: Osijek; 2003. p. 91-9
- [7] Duan, Z., Liu, J., Tuo, Y., Chiogna, G., Disse, M.: Evaluation of eight high spatial resolution gridded precipitation products in Adige Basin (Italy) at multiple temporal and spatial scales, SCIENCE OF THE TOTAL ENVIRONMENT, Elsevier B.V.; 573 (2016) September, pp. 1536-53, https://doi.org/10.1016/j.scitotenv.2016.08.213

years, which is evident from the comparison of the mean monthly precipitation above the basin (Figure 4 - graphs 15 and 16).

5. Conclusion

An alternative approach to hydrological modelling is presented in this paper, for cases in which the number of precipitation stations in the catchment area or in the immediate vicinity is insufficient, or when the existing time series have interruptions in measurements. In such complicated situations, a remotely sensed product with global coverage, i.e. CHIRPS, could be a valid replacement for meteorologically measured precipitation. It should be noted that the reliability of such models is slightly lower compared to the model in which precipitation observed at weather stations and/or precipitation stations is used as an input parameter, bearing in mind that the Bednja basin is very well covered by the DHMZ gauge network. The question of the situation in the basins where the density of precipitation gauge stations is lower remains open, which is a topic for further research. According to the obtained results, it can be assumed that the accuracy could be further improved by calibrating the original model over a longer time period of precipitation observed at weather stations and/or precipitation stations.

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- [8] Funk, C.C., Peterson, P.J., Landsfeld, M.F., Pedreros, D.H., Verdin, J.P., Rowland, J.D.: A quasi-global precipitation time series for drought monitoring: U.S. Geological Survey Data Series 832, Https://pubs.usgs.gov/ds/832/pdf/ds832.pdf %OAhttps://pubs. er.usgs.gov/publication/ds832Usgs. Reston, VA; 2014, https://doi. org/10.3133/ds832
- [9] Arnold, J.G., Srinivasan, R., Muttiah, R.S., Williams, J.R.: Large area hydrologic modeling and assessment part I: Model development, Journal of the American Water Resources Association, 34 (1998) 1, pp. 73-89, https://doi.org/10.1111/j.1752-1688.1998.tb05961.x
- [10] Abbaspour, K.C., Rouholahnejad, E., Vaghefi, S., Srinivasan, R., Yang, H., Kløve, B.: A continental-scale hydrology and water quality model for Europe: Calibration and uncertainty of a high-resolution large-scale SWAT model, Journal of Hydrology, Elsevier B.V.; 524 (2015) pp. 733-52, https://doi.org/10.1016/j.jhydrol.2015.03.027
- [11] Bosch, N.S., Allan, J.D., Dolan, D.M., Han, H., Richards, R.P.: Application of the Soil and Water Assessment Tool for six watersheds of Lake Erie: Model parameterization and calibration, Journal of Great Lakes Research, 37 (2011) 2, pp. 263-71, https:// doi.org/10.1016/j.jglr.2011.03.004
- [12] Shrestha, S., Sharma, S., Gupta, R., Bhattarai, R.: Impact of global climate change on stream low flows: A case study of the great Miami river Watershed, Ohio, International Journal of Agricultural and Biological Engineering, 12 (2019) 1, pp. 84-95

Evaluation of remotely sensed precipitation product in a hydrological model of the Bednja watershed

- [13] Tuo, Y., Duan, Z., Disse, M., Chiogna, G.: Evaluation of precipitation input for SWAT modeling in Alpine catchment: A case study in the Adige river basin (Italy), Science of the Total Environment, 573 (2016) pp. 66-82
- [14] Grusson, Y., Anctil, F., Sauvage, S., Sánchez Pérez, J.: Testing the SWAT Model with Gridded Weather Data of Different Spatial Resolutions, Water, 9 (2017) 1, pp. 54, https://doi.org/10.3390/ w9010054
- [15] Glavan, M., Flajsig, G.Ć., Karleuša, B., Vučković, I.: Modelling diffuse and point source pollution risks in the case of transboundary Sotla river basin, SWAT model conference, (2017) pp. 79
- [16] Počakal, M.: Hidrografske veličine porječja Bednje, Geografski glasnik, 44 (1982), pp. 85-102
- [17] Šimunić, A., Pikija, M., Hećimović, I.: Osnovna geološka karta SFRJ 1:100.000 s tumačem - list Varaždin, Geološki zavod Zagreb: Zagreb; 1978.
- [18] Aničić, B., Juriša, M.: Osnovna geološka karta SFRJ 1:100.000 list Rogatec, Institut za geološka istraživanja Zagreb, Geološki zavod Ljubljana, Savezni geološki zavod Beograd; 1983. pp. 33-68
- [19] Dragičević, I., Blašković, I., Mayer, D., Žugaj, R., Tomljenović, B.: Gorski i prigorski vodonosnici sjeverne Hrvatske (izvješće o radovima u 1996. godini), Fond stručne dokumentacije RGNF: Zagreb; 1997.
- [20] Šimunić, A.: Geološka Građa Okolice Lepoglave I Osvrt Na Pojave Mineralnih Sirovina, Radovi Zavoda za znanstveni rad JAZU, 1 (1986) 1, pp. 19-32
- [21] Marković, T., Larva, O., Brkić, Ž., Dolić, M., Kuhta, M.: Stanje podzemnih voda na vodnom području rijeke Dunav s obzirom na prirodan sadržaj metala i njihov antropogeni utjecaj, Hrvatski geološki institut: Zagreb; 2015.
- [22] Brkić, Ž., Larva, O., Marković, T.: Ocjena stanja i rizika cjelina podzemnih voda u panonskom dijelu Republike Hrvatske, Hrvatski geološki institut: Zagreb; 2009.
- [23] Zaninović, K., Gajić-Čapka, M., Perčec Tadić, M., Vučetić, M., Milković, J., Bajić, A., Cindrić, K., Cvitan, L., et al.: Klimatski atlas Hrvatske, Climate atlas of Croatia: 1961. - 1990.: 1971. - 2000., Državni hidrometeorološki zavod: Zagreb; 2008.
- [24] DHMZ.: Meteorološki podaci 2000. 2018., Zagreb; 2020
- [25] Arnold, J.G., Moriasi,D.N., Gassman, P.W., Abbaspour, K.C., White, M.J., Srinivasan, R., et al.: SWAT: Model Use, Calibration, and Validation, Transactions of the ASABE, 55 (2012) 4, pp. 1491-508, https://doi.org/10.13031/2013.42256
- [26] Arnold, J.G., Srinivasan, R., Muttiah, R.S., Allen, P.M.: Continental scale simulation of the hydrologic balance, Journal of the American Water Resources Association, 35 (1999) 5, pp. 1037-1051, https://doi.org/10.1111/j.1752-1688.1999.tb04192.x
- [27] Panagos, P., Van Liedekerke, M., Jones, A., Montanarella, L.: European Soil Data Centre: Response to European policy support and public data requirements, Land use Policy, 29 (2012) 2, pp. 329-338, https://doi.org/10.1016/j.landusepol.2011.07.003
- [28] Funk, C., Peterson, P., Landsfeld, M., Pedreros, D., Verdin, J., Shukla, S., et al.: The climate hazards infrared precipitation with stations - A new environmental record for monitoring extremes, Scientific Data, 2 (2015) 1, pp. 1-21, https://doi.org/10.1038/ sdata.2015.66
- [29] Saha, S., Moorthi, S., Pan, H.L., Wu, X., Wang, J., Nadiga, S., et al.: The NCEP climate forecast system reanalysis, Bulletin of the American Meteorological Society, 91 (2010) 8, pp. 1015-1057

- [30] Dile, Y.T., Srinivasan, R.: Evaluation of CFSR climate data for hydrologic prediction in data-scarce watersheds: An application in the Blue Nile river basin, Journal of the American Water Resources Association, 50 (2014) 5, pp. 1226-41, https://doi.org/10.1111/ jawr.12182
- [31] Fuka, D.R., Walter, M.T., Macalister, C., Degaetano, A.T., Steenhuis, T.S., Easton, Z.M.: Using the Climate Forecast System Reanalysis as weather input data for watershed models, Hydrological Processes, 28 (2014) 22, pp. 5613-5623, https://doi.org/10.1002/ hyp.10073
- [32] Roth, V., Lemann, T.: Comparing CFSR and conventional weather data for discharge and soil loss modelling with SWAT in small catchments in the Ethiopian Highlands, Hydrology and Earth System Sciences, 20 (2016) 2, pp. 921-934, https://doi. org/10.5194/hess-20-921-2016
- [33] Abbaspour, K.C., Vejdani, M., Haghighat, S.: SWAT-CUP calibration and uncertainty programs for SWAT, MODSIM07 - Land, Water and Environmental Management: Integrated Systems for Sustainability, Proceedings, (2007), pp. 1596-1602
- [34] Nash, J.E., Sutcliffe, J.V.: River flow forecasting through conceptual models part I - A discussion of principles, Journal of Hydrology, 10 (1970) 3, pp. 282-290, https://doi.org/10.1016/0022-1694(70)90255-6
- [35] Moriasi, D.N., Arnold, J. G., Van Liew, M.W., Bingner, R.L., Harmel, R.D., Veith, T.L.: Model Evaluation Guidelines for Systematic Quantification of Accuracy in Watershed Simulations, Transactions of the ASABE, 50 (2007) 3, pp. 885-900, https://doi. org/10.13031/2013.23153
- [36] Rahman, K., Maringanti, C., Beniston, M., Widmer, F., Abbaspour, K., Lehmann, A.: Streamflow Modeling in a Highly Managed Mountainous Glacier Watershed Using SWAT: The Upper Rhone River Watershed Case in Switzerland, Water Resources Management, 27 (2013) 2, pp. 323-339, https://doi.org/10.1007/ s11269-012-0188-9
- [37] Duru, U., Arabi, M., Wohl, E.E.: Modeling stream flow and sediment yield using the SWAT model: a case study of Ankara River basin, Turkey, Physical Geography, 39 (2018) 3, pp. 264-89, https://doi. org/10.1080/02723646.2017.1342199
- [38] Abbaspour, K.C., Yang, J., Maximov, I., Siber, R., Bogner, K., Mieleitner, J., et al.: Modelling hydrology and water quality in the pre-alpine/alpine Thur watershed using SWAT, Journal of Hydrology, 333 (2007) 2-4, pp. 413-430
- [39] Abbaspour, K.C., Johnson, C.A., van Genuchten, M.T.: Estimating Uncertain Flow and Transport Parameters Using a Sequential Uncertainty Fitting Procedure, Vadose Zone Journal, 3 (2004) 4, pp. 1340-1352, https://doi.org/10.2136/vzj2004.1340
- [40] Krige, D.G.: A Statistical Approach to Some Basic Mine Valuation Problems on the Witwatersrand, Journal of the Chemical, Metallurgical and Mining Society of South Africa, Southern African Institute of Mining and Metallurgy; 52 (1952) 6, pp. 201-215
- [41] Piniewski, M., Okruszko, T.: Multi-Site Calibration and Validation of the Hydrological Component of SWAT in a Large Lowland Catchment, In: Świątek D, Okruszko T, editors. Modelling of Hydrological Processes in the Narew Catchment, Springer-Verlag: Berlin; 2011. p. 15-41, https://doi.org/10.1007/978-3-642-19059-9_2
- [42] Čerkasova, N., Umgiesser, G., Ertürk, A.: Development of a hydrology and water quality model for a large transboundary river watershed to investigate the impacts of climate change - A SWAT application, Ecological Engineering, Elsevier; 124 (2018) October, pp. 99-115, https://doi.org/10.1016/j.ecoleng.2018.09.025

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- [43] Abbaspour, K.C., Vaghefi, S.A., Srinivasan, R.: A guideline for successful calibration and uncertainty analysis for soil and water assessment: A review of papers from the 2016 international SWAT conference, Water (Switzerland), 10 (2017) 1, pp. 1-18
- [44] Meng, X., Wang, H., Lei, X., Cai, S., Wu, H., Ji, X., et al.: Hidrološko modeliranje u porječju rijeke Manas primjenom alata za procjenu tla i vode pomoću CMADS-a, Tehnicki Vjesnik, 24 (2017) 2, pp. 525-534
- [45] Abbaspour, KC.: SWAT-CUP: SWAT calibration and uncertainty programs-a user manual, Swiss Fed. Inst. Aquat. Sci. Technol. Eawag. Swiss Federal Institute of Aquatic Science and Technology: Dübendorf; 2011. p. 106
- [46] Neitsch, S.L., Arnold, J.G., Kiniry, J.R., Williams., J.R.: Soil and Water Assessment Tool User's Manual Version 2005., Http://repository. tamu.edu/handle/1969.1/128050Texas Water Resour. Inst. Tech. Rep. No. 406. Texas Water Resources Institute: Temple, Texas; 2011.